# Introduction to Vermont's Equalization Study \& Certified Sales 

# Division of Property Valuation and Review Vermont Department of Taxes 

## 2018 Course Training Materials

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## II. Ratio Study Basics

All sales to be included in the sales study must meet: sales from the last 3 years, verified "Arms-Length" transactions, and sufficient amount of data to be able to stratify.

The formula used:

## Assessed Value / Sales Price = Calculated Ratio

With the Data Set calculate: measures of central tendency, uniformity in the results, and analyze the results for sampling errors.

Assumption 1: same assessment practices for sold and unsold properties
Assumption 2: assessed values and sale prices are independent opinions of value



The following graph represents:

- Each point represents two independent estimates of a town's grand list value,
- Degree of association measured by R-Squared - a value of 1.0 or $100 \%$ would indicate perfect predictability; 0 would mean no relationship,
- The value in excess of $99 \%$ suggests an extremely high level of association, and
- Towns can use ratio studies to fine tune CAMA models for individual properties


## III. Sales Report

## Ratios

Compare listed values to sales price for individual ratios, group ratios and overall Level of Appraisal ratios. This can be entered or exported, arranged, sorted, calculated and maintained using an excel spreadsheet.


Final Computation Sheet


Sales Analysis
LEVEL OF APPRAISAL / ASSESSMENT CALCULATION

| CATEGORY | PARCEL | SALE DATE | SALE PRICE | LISTED VALUE | ASSESS RATIO | ABS DEV FROM MEDIAN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| R1 | 30306 | 06/18/2008 | \$300,000 | \$229,500 | 76.50\% | 22.85 |
| R1 | 20201 | 11/09/2008 | \$99,500 | \$95,300 | 95.78\% | 3.57 |
| R1 | 20202 | 10/24/2009 | \$90,900 | \$96,300 | 105.94\% | 6.59 |
| R1 | 30307 | 08/20/2009 | \$125,000 | \$57,700 | 46.16\% | 53.19 |
| R2 | 45674 | 04/22/2009 | \$230,000 | \$228,500 | 99.35\% | 00.00 |
| R2 | 54321 | 03/27/2009 | \$189,000 | \$165,200 | 87.41\% | 11.94 |
| R2 | 42413 | 08/03/2009 | \$220,000 | \$180,200 | 81.91\% | 17.44 |
| R2 | 45679 | 09/09/2008 | \$110,000 | \$87,000 | 79.09\% | 20.26 |
| R2 | 45453 | 05/19/2009 | \$215,000 | \$140,700 | 65.44\% | 33.91 |
| R2 | 12121 | 04/01/2009 | \$190,000 | \$190,600 | 100.32\% | . 97 |
| R2 | 89806 | 06/16/2008 | \$354,000 | \$355,600 | 100.45\% | 1.10 |
| R2 | 45671 | 06/29/2009 | \$471,000 | \$472,300 | 100.28\% | . 93 |
| MHL | 45673 | 08/13/2009 | \$60,000 | \$63,200 | 105.33\% | 5.99 |
| V1 | 11113 | 08/01/2009 | \$152,000 | \$148,000 | 97.37\% | 1.98 |
| V1 | 23232 | 08/21/2009 | \$150,000 | \$127,800 | 85.20\% | 14.15 |
| V2 | 11116 | 06/12/2009 | \$64,000 | \$66,400 | 103.75\% | 4.40 |
| V2 | 12128 | 08/31/2009 | \$145,000 | \$144,800 | 99.86\% | . 51 |
| V2 | 23269 | 06/12/2009 | \$209,000 | \$131,200 | 62.78\% | 36.57 |
| WOOD | 11115 | 08/31/2008 | \$59,500 | \$50,700 | 85.21\% | 14.14 |
| MISC | 29287 | 04/29/2009 | \$25,000 | \$40,800 | 163.20\% | 63.85 |
| MISC | 64632 | 02/13/2009 | \$25,000 | \$33,700 | 134.80\% | 35.45 |
| MISC | 90967 | 05/01/2009 | \$30,000 | \$30,900 | 103.00\% | 3.65 |
| MISC | 78790 | 07/08/2008 | \$49,900 | \$57,600 | 115.43\% | 16.08 |
| ** |  | SUM | \$3,563,800 | \$3,194,000 | 57,600/49,900= Individual Ratio <br> $3,194,000 / 3,563,800=89.62$ LOA <br> Total Listed Value $/$ Total Sale Price $=L O A$ |  |
|  |  | LOA |  | 89.62\% |  |  |
|  |  | MEDIAN |  | 99.35\% |  |  |
|  |  | COUNT |  | 23 |  |  |
|  |  | TOTAL DEV |  | 369.52 |  |  |
|  |  | AVG DEV |  | 16.07 |  |  |
|  |  | COD |  | 16.17 |  |  |

*Individual Ratio= Listed Value/Sales Price = highlight cell/highlight cell (then copy command down entire column)
*Level of Appraisal = Total Listed Value/Total Sales Price
for each column (listed value and sales price) type in =sum(highlight all columns)
*Copy categories to individual worksheets (pages in spreadsheet) by clicking on Insert and then Worksheet, then go to the bottom tabs and right click to rename the tab.
*Then highlight all sales info for that category and copy to the second worksheet (page).
*Then set up your calculations for that page of information similar to this.
*Median- type in =Median (highlight ratio cells).
*Count- type in =Count (highlight any column with values)
*Add a column for Absolute Deviation from the Median- in first cell of this column type in =ABS (highlight your ratio cell-
Median cell)
*Put a dollar sign in between the letter of the cell and the number (for Median) to tell it to repeat this cell.
*Then you can copy this formula using copy and paste all the way down the column.
*Calculate a Sum of absolute deviations =SUM (highlight cells) for deviation.
*Calculate an Average Deviation =sum of deviations/count
*COD =Average Absolute Deviation/Median*100

Sales Summary Report



Explanation of the Sales Summary Report

| Top Center of Page - Reliable Estimator |  |  |
| :---: | :---: | :---: |
| Town Sample <br> Valid? | YES | (90\% confident that true aggregate ratio is within 10\% of sample |
| ratio. ${ }^{*}$ ) |  |  |


| Left Third of Page - Descriptive Statistics |  |
| ---: | :---: |
| 136 | Transactions (Includes Outliers/Extremes) |
| 390,744 | Average Sales Price |
| 381,349 | Average Listed Value |
| 100.13 | Average Ratio |
| 100.00 | Median Ratio |
| 50.06 | Low Ratio |
| 166.67 | High Ratio |
| 1.03 | Price Related Differential (Regression Index) |
| 13.53 |  |
| 19 | COD |
| $14 \%$ | Percent of Transactions with Assessment Ratio Between .98 and 1.02 |


| Middle Third of Page - Trimming |  |  |  |
| ---: | :---: | :--- | :--- |
| Original Data (All Valid Sales Transactions) |  |  |  |
| 89.40 | Low InterQuartile Value |  |  |
| 110.26 | Hi InterQuartile Value |  |  |
| 20.86 | InterQuartile Range |  |  |
| 58.11 | Value of Outlier Low Limit |  | Number of Low Outliers |
| 141.55 | Value of Outlier High Limit |  | Number of Hi Outliers |
| 26.82 | Value of Extreme Low Limit |  | Number of Low Extremes |
| 172.84 | Value of Extreme High Limit |  | Number of Hi Extremes |


| Right Third of Report - Estimator |  |
| ---: | :---: |
|  | RATIOS and CONFIDENCE INTERVALS |
| 94.71 | (Trimmed Data) |
| 100.48 | Low 90 Percent Value of Aggregate |
| 97.60 | Hi 90 Percent Value of Aggregate |
| $2.95 \%$ | Aggregate Ratio |
| 20.88 | $\left(^{*}\right)$ Sampling Error |

104.73 Low InterQuartile Value (1 $\sigma$ )
130.40 High InterQuartile Value (1 $\sigma$ )
25.67 InterQuartile Range
130.40 High InterQuartile Value

- 104.73 Low InterQuartile Value 25.67


### 66.23 Value of Outlier Low Limit

104.73 Low InterQuartile Value

- $\quad 38.51$ InterQuartile Value Times 1.5 (number above in red x 1.5)
66.23 Value of Outlier Low Limit
168.91 Value of Outlier High Limit 130.40 High InterQuartile Value
$+\quad 38.51$ InterQuartile Value Times 1.5 (number above in red $\times 1.5$ ) 168.91 Value of Outlier High Limit
27.72 Value of Extreme Low 104.73 Low InterQuartile Value
- $\quad 77.01$ InterQuartile Value Times 3 (number above in red $\times 3$ )
27.72 Value of Extreme Low (anything lower will not be used in study)
207.41 Value of Extreme High Limit 130.40 High InterQuartile Value
$+\quad 77.01$ InterQuartile Value Times 3 (number above in red $x$ 3) 207.41 Value of Extreme High Limit (anything higher will not be used in study)


## IV. Coefficient of Dispersion

- The coefficient of dispersion is a measurement of uniformity of appraised values and can be a measure of the quality of the assessment process.
- The steps in the computation of the coefficient of dispersion are:
o Find the difference, or absolute deviation (disregarding the plus or minus), between each individual assessment ratio (sales ratio) measured against the median ratio. Sum these differences for total absolute deviation.
o Divide the sum of the deviation, or differences, by the total number of properties sold to locate the average absolute deviation.
o Divide the average absolute deviation by the median ratio and multiply this result by 100.
- The resultant coefficient of dispersion, also known as the "index of assessment inequality," is the percentage by which the various individual assessment sales ratios differ, on the average, from the median ratio.
Illustration:


Coefficient of Dispersion
0.00-9.90\%
10.00-19.90\%
20.00\% and above

Uniformity of Assessment
Excellent
Reasonable (closer to 20 should be monitored by town) Exceeds statutory benchmarks \& triggers Reappraisal Order

The relative difficulty of the assessment problem is an important factor to be considered in the comparison of coefficients of dispersion between areas and among classes of property. It is reasonable to expect a higher degree of equality in those areas with homogeneous properties to be assessed. Conversely, a lesser degree of uniformity is to be anticipated in those areas with a greater variety of properties. Land is a good example of this and an absence of market criteria.

## Statistical Extremes are not used to calculate Coefficient of Dispersion (COD).

## Common Level of Assessment / Appraisal Calculation



Column $D=$ Listed Value divided by Sale Price (=C3/B3, C4/B4, C5/B5, etc)
(enter this calculation and then
copy down)

B16= Total of all Sale Prices (=sum(B3:B13)) 1,772,650

C16= Total of all Listed Values (=sum(C3:C13)) 1,681,700

Median Ratio= Median of all Ratios 100\%
(=Median(D3:D13))

Count= Total number of samples (=Count(B3:B13))*
*any column will work as long as you only include those with data for a correct count) $=11$

(enter this calculation and then
copy down)

| Total Deviation= Total of all deviations (=sum | 86.00 |
| :--- | :---: |
| (E3:E13)) |  |
| Average Deviation= Average of all deviations | 7.82 |
| (=E16/C19) |  |

$\mathrm{COD}=\quad$ Average Deviation/Median Ratio (=E17/C18) $\times 100 \quad(7.82 / 100) \times 100=7.82$

## What Does a COD Tell Me?

- If the COD of less than $5 \%$ is an indicator of Sales Chasing.
- If it's to high there is a high degree inequity in your town.
- $20 \%=100$ points spread for $95 \%$ of the ratios (i.e. 50 to 150 points)
- A reasonable range $7 \%$ to $17 \%+/-$
- Not only the Town Level can be useful also look as individual categories and classes


## V. Identify Internal Inequity

- Use the categories and classes
- Recent reappraisal or "good" CLA /
- COD no guarantee of equity
- Compare mean, median and aggregate ratios
- Investigate further if more than ten points difference
- Caution: difference may not be significant if small sample size and /or high variability
- Particular attention if on opposite sides of split grand list (i.e., nonresidential open land versus residences)
- Internally equitable grand lists equalize well

- Measure = PRD (Price-Related Differential)
- Ratio of mean to weighted mean
- Regressive (PRD > 1.03) = Higher value properties are assessed proportionally lower than lower value properties.
- Progressive (PRD < 0.98) = Lower value properties are assessed proportionally lower than higher value properties.
- In Vermont, most samples are slightly to severely regressive. A scatterplot of ratios versus sale price shows a downward slope - higher value sales have lower ratios.
- Problem if over 110

- PRD is 125
- Parcels selling under $\$ 50,000$ assessed around $130 \%$ of market value
- Parcels selling over \$350,000 assessed around $70 \%$ of market value
- Tax burden almost double on lower value parcels


## Glossary of Terms

Accuracy - it is a description of systematic errors, a measure of statistical bias; as these cause a difference between a result and a "true" value, International Organization for Standardization (ISO) calls this trueness.

Aggregate Ratio - In the equalization study, the figure you get when the sum of the assessments is divided by the sum of the sale prices. May also be called the weighted mean or the weighted average ratio.

Category (see also use class) - All taxable properties in Vermont are classified into 15 categories based on their use. For example, R1 refers to small acreage residential and UE to utility electric. The goal is to group properties with similar uses together.

Class (see also use class) - There are 4 classes of property that are formed by the aggregation of the 15 categories into like-use groups. They are residential (R1, R2, MHU, MHL, V1 and V2), commercial / industrial (COMM, CMA and IND), utilities (UE and UO), and open land (Farm, Wood and MSC).

Coefficient of Dispersion (COD) - The COD is a measure of uniformity of appraisals for all properties on the grand list. If, for example, a town has valued every single property at $100 \%$ of fair market value (that is, every property has an assessment to fair market value ratio of $100 \%$ ), then there is zero dispersion, hence 0.00 percent COD. Similarly, if every single property is assessed at $80 \%$ of fair market value, there is zero dispersion. If, however, the town median assessment to sales ratio is $80 \%$, but individual assessments vary markedly, either above or below the median, then the disparity of assessments will reflect in a COD greater than 0\%. As the disparity increases, the COD correspondingly increases.

Zero is a perfect score as a coefficient of dispersion. It indicates absolute fairness insofar as every taxpayer is appraised at exactly the same percentage of fair market value. The higher the number, the greater the dispersion, or disparity, in how properties are assessed in that town. Because of fluctuations in the market, and because properties are constantly being improved or changed, a perfect score is close to impossible. A coefficient of dispersion of 10 or lower is excellent. Statistically, it is the average deviation of a group of RATIOS from the TOWN-WIDE MEDIAN expressed as a percentage of the MEDIAN.

The statutory definition is in 32 VSA, $\S 5401(1)$. Vermont municipalities will be required to reappraise when the COD falls above 20\%. 32 VSA , § 4041a.

Common Level of Appraisal (CLA) - In Vermont law, "the ratio of the aggregate value of local education property tax grand list to the aggregate value of the equalized education property tax grand list." 32 VSA, $\S 5401(3)$. It is essentially a measure of how close a town or city's local appraisals are to fair market value. Vermont municipalities are required to reappraise when the CLA falls below $80 \%$. 32 VSA , section 4041a.

Confidence Interval (see also confidence level) - An interval calculated around the aggregate ratio. The high and low values in the interval form a range within which one can predict (within the limits of the confidence level) that the true ratio for the grand list exists. Vermont's study required that the interval not exceed a range of plus and minus $10 \%$ around the aggregate ratio. This is the maximum range of the interval. The actual range is generally considerably less but will depend on the size of the sales sample and its variability.

Confidence Level (see also confidence interval) - The required level of confidence to achieve a preestablished level of statistical reliability. Vermont's study is based on a $90 \%$ confidence level. This means that if we were to repeatedly select sales samples from a grand list, the resulting equalization ratios would be within the calculated confidence interval 9 out of 10 times. Ratios used for equalization are calculated at the lowest level of sales aggregation (see also category, class, town-wide and use class) that achieves the $90 \%$ level.

Extreme Ratios (see also outlier ratios and interquartile range) - Extreme ratios are those identified as being markedly higher or lower than the aggregate ratio. If a ratio is identified as being extreme, its inclusion in the study would distort the results. Extreme ratios are therefore not used to calculate study results at any level of aggregation where they are identified.

Level of Appraisal (LOA) - Either a smaller sample of properties $\& /$ or lesser timeframe than the State Standards and doesn’t include Current Use \& Utility adjustments.

International Association of Assessing Officers (IAAO) - A non-profit educational association whose mission is to promote innovation and excellence in property appraisal and property tax policy and administration through professional development, education, research, and technical assistance.

Interquartile Values/Range (see also outlier and extreme ratios)- The values that divide a set of ratios into 4 equidistant parts with the lowest observation equal to $0 \%$ and the highest equal to $100 \%$. The interquartile range is the distance from the 25th percentile to the 75th percentile. These statistics are used to identify outlier and extreme observations. An outlier is defined as a ratio that is beyond 1.5 times the interquartile range from either the 25 th or the 75 th percentiles. An extreme is defined as a ratio that is beyond 3 times the interquartile range from the same percentiles.

Mean - The result of adding all the values and dividing by the number of values. For instance, the mean of 3,5 and 10 is $6 .(3+5+10=18 ; 18 / 3=6$. $)$ Also called the arithmetic mean or the average.

Median Ratio - The midpoint or middle value when a set of values is ranked in order of magnitude; if the number of values is even, the midpoint or average of the two middle values.

Mode - the most frequent value in the data set. This is the only central tendency measure that can be used with nominal data, which have purely qualitative category assignments.

Outlier Ratio (see also extreme ratio and interquartile range) - Ratios that are found to be statistically different from other sales ratios in a given sample. Outliers may deserve special attention depending on the variability of other sales ratios in the sample.

Precision - is a description of random errors, a measure of statistical variability.
Price-Related Differential (PRD) - The mean ratio divided by the aggregate ratio. Also called the regressivity index. This statistic is used to determine whether assessment practices are progressive or regressive. A PRD above 1.03 tends to indicate assessment regressivity (lower valued properties are assessed at a higher ratios). A PRD below .98 tends to indicate assessment progressivity (higher valued properties are assessed at a higher ratios).

Reliable Ratio (see also confidence level and confidence interval) - A ratio which is statistically accurate within a margin of error of plus or minus $10 \%$ at a $90 \%$ confidence level. The sale report indicates if this guideline was met at each level of sales aggregation.

Townwide (see also use class) - The highest level of sales sample aggregation in which all sales across all categories are included for a city or town.

Trimmed Data (see also extreme ratios) - This refers to the data used to calculate the equalization ratio (i.e., the aggregate or weighted mean) and its confidence interval after any extreme ratios have been eliminated.

Use Class - The classification of properties into groups based on their use. For example, residential, commercial, utility etc. All properties in Vermont are grouped into 15 categories. In conducting the equalization study, listed value to sale price ratios are calculated at the lowest level of aggregation that achieves a reliable ratio (see also reliable ratio). If a reliable ratio cannot be achieved at the category level, then the next higher level of aggregation (class) is used. If a reliable ratio is not achieved at this level, then the townwide ratio is used for equalization.

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December 18, 2017

Town Clerk
Town of Andover
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Andover, VT 05143

## 2017 Equalization Study Results

This letter serves as notification of the results of Property Valuation and Review (PVR)'s 2017 equalization study. Every year we are required to certify the equalized education property value (EEPV or EEGL) and coefficient of dispersion (COD) for each Vermont town. 32 V.S.A § 5406. This letter also communicates the Common Level of Appraisal (CLA) for your town and explains how it will impact your homestead and nonresidential education tax rates.

| Education Grand List (from 411): | $\$ 166,896,400$ |  |
| :--- | :--- | ---: |
| Equalized Education Grand List (EEGL): | $\$ 139,111,020$ |  |
| Common Level of Appraisal (CLA): | $\mathbf{1 1 9 . 9 7} \%$ or $\mathbf{1 . 1 9 9 7}$ |  |
| Coefficient of Dispersion (COD): | $\mathbf{9 . 6 7 \%}$ |  |

The education grand list listed here is what was reported by your town to the state on the 411 form with your town's cable (if applicable) and tax increment financing (TIF) amounts (if any) included. This number represents the town's total property value that is subject to the education property tax (from the most recent grand list available) and serves as the numerator in the computation of the CLA. Please note: tax revenue from any TIF property value is subject to allocation. 32 V.S.A. § 5404a.

The equalized education grand list (EEGL) represents PVR's statutorily-mandated estimate of total fair market value of the education grand list in your town and serves as the denominator in the computation of the CLA. To find out more about how the equalization study is conducted, how to read the certified sales report, and additional instructions on how to appeal your results, please see the "Introduction to Vermont's Equalization Study" document at:

## tax.vermont.gov/research-and-reports/reports/equalization-study

The common level of appraisal (CLA) is determined by dividing the education grand list by the equalized education grand list. 32 V.S.A. § 5401 . A number over $100 \%$ indicates that property in your town is generally listed for more than its fair market value. A number less than $100 \%$ indicates that property is generally listed for less than its fair market value. A CLA below $80 \%$ necessitates a reappraisal. 32 V.S.A § 4041a. The homestead and nonresidential tax rates in your town will be adjusted by your town's CLA. 32 V.S.A $\S 5402$. The nonresidential rate in your town will be the statewide
nonresidential rate divided by your CLA. The homestead rate will be the town homestead rate (which is determined by the per-pupil spending of any school districts) to which your town belongs) divided by the CLA. A CLA greater than $100 \%$ will result in a downward adjustment of tax rates, and a CLA less than $100 \%$ will result in upward adjustment.

To get answers to many common questions about tax rates and how they are determined, please see: tax.vermont.gov/research-and-reports/tax-rates-and-charts/education-tax-rates/faqs

To see how the per-pupil spending of the districts) to which your town belongs is calculated and how that, along with your town's CLA, makes the tax rates, please see the tax rate calculations link at: tax.vermont.gov/property-owners/understanding-property-taxes/education-tax-rates

The coefficient of dispersion (COD) is a measure of how fairly distributed the property tax is within your town. It is calculated as the average of the (absolute) difference of each sales ratio (list price divided by sales price) in the study from the median ratio. That result is then divided by the median ratio to get the COD, which is expressed as a percent. 32 V.S.A. § 5401. A high COD means that within your town many taxpayers are paying more than their fair share and many are paying less than their fair share. A COD over 20\% necessitates a reappraisal. 32 V.S.A. § 4041a.

Appeals: A municipality may petition the director of Property Valuation and Review for a redetermination of its EEPV and/or COD. 32 V.S.A § 5408. All petitions must be in writing and signed by the chair of the municipality's legislative body. Petitions should contain a plain statement of matters being appealed and a statement of the remedy being sought. Petitions must be received by PVR by the close of business on the 35th day after mailing of this letter. Additional instructions on appeals can be found in the "Introduction to Vermont's Equalization Study" document at:
tax.vermont.gov/research-and-reports/reports/equalization-study
If you have any questions, please contact your district advisor or call 802-828-5860. For a copy of your town final computation sheet and certified sales report, please see:

## tax.vermont.gov/research-and-reports/reports/equalization-study

Sincerely,


Jill Remick, Acting Director
Property Valuation and Review

cc: Chair, Board of Listers<br>Chair, School Board<br>Chair, Select Board<br>Superintendent of Schools

